

File: ISIS-PG-FMT511\_cheXX\_dat.pdf

Narrative description of Randlsq program main printout (general file format) 'cheXX.dat', where XX denotes the run-number ID for the best-fit solution from RAND, which was retained for that particular body. These run-number IDs are fortunately unique between each of the measured Saturnian moons such that XX: 03=Mimas, 04=Dione, 05=Iapetus, 06=Tethys, 07=Rhea, 14=Enceladus. Note, this input format is identical to the Randlsq program output file format.

Created as part of a project to put planetary geodesy control networks on the web. These control networks are from ISIS Planetary Geodesy Software (formerly RAND/USGS Planetary Geodesy (RUPG) Software).

Version: 2015.10.05

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Filename: cheXX.dat (example: che04.dat)

The following is a general guide to the solution "general printout" output that is generated by the randlsq program. The "Group" designations here are meant to be a general guide to the different sections of that output.

The examples below are taken from the file "che04.dat".

Group 1 - General description of solution parameters.  
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Number of images (NPIC), number of control points (NPOI), number of image measures (line and sample) (NMEA), and number of unknowns (NUNK). This is followed by a list of the types of parameters being solved for.

Example (from che03.dat):

INITIAL CONFIGURATION FOR THESE DATA

NPIC = 32 NPOI = 109 NMEA = 672 NUNK = 314

SOLVING FOR CORRECTIONS TO LATITUDES OF POINTS  
SOLVING FOR CORRECTIONS TO LONGITUDES OF POINTS  
SOLVING FOR CORRECTIONS TO ALPHA C-MATRIX ANGLES  
SOLVING FOR CORRECTIONS TO DELTA C-MATRIX ANGLES  
SOLVING FOR CORRECTIONS TO KAPPA C-MATRIX ANGLES

Group 2 - Parameter Weights in RAND Scheme  
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These are parameter weights, as used by the original RAND weighting scheme. Numbers are simply listed in solved for order, from parameter number 1 to parameter number NUNK. (The order is as specified in the

list of types of parameters in "group 2" above, i.e. latitude, longitude, radii of point 1, then point 2, etc., then the three angles for image 1, then image 2, etc.) A "20" here indicates the parameter is fixed (e.g. weighted with a value of  $10^{20}$ ). A "-38" here indicates the parameter is free (weighted with a value of  $10^{-38}$ ).

(Note that a bug currently exists that when angle weighting is done (IAWT=1) or control point weighting is done (from the a priori input file) this listing will not show the correct weights for camera angle parameters or control point parameters, respectively, as the printout is done before those weights have been applied.)

Example (from che03.dat):

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                                WEIGHTS
-38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -
38 -38
-38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -
38 -38
-38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -
38 -38
-38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -38 -
38 -38
etc.
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Group 3 - Iteration Output  
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The output from each iteration of the program follows. For each iteration there are two sub-groups of output, with one (Group 4A) being the measurement residuals, and the other (Group 4B) being the solution statistics for the current iteration.

Note that the first set of (Group 4A and 4B) output is actually from the "zeroth" iteration of the program, i.e. it is a simple calculation of the residuals (observed minus computed) values, but derived only from the a priori values before any solution is done. The (4B) statistics are actually the statistics for these residuals only and not a solution. In other words, this set of residuals and the statistics only show how well the a priori information actually matches the measurement data before a solution is done.

After that printout, an actual least squares solution is done, and the next and succeeding sets of output are all from actual solutions. Therefore, if "nit" iterations are specified in the program control file (see file ISIS-PG-FMT101.doc or .pdf for format), then the actual number of least squares solution iterations will be NIT-1.

Group 3A - Residual output from the current iteration  
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Shown for each line and sample measurement from the input mm measurement file, are the image number, the control point number, the X or SAMPLE residual (mm), and Y or LINE residual (mm).

Example (from che03.dat):

PICTURE	POINT	XO-XC	YO-YC
3492903	50	-0.00518	-0.00386
3492903	53	0.01341	0.02260
3492903	61	-0.01484	0.01150
3492903	62	0.00761	0.00095
3492903	63	0.00065	-0.01979

etc.

Group 3B - Residual or Solution Statistics.  
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Next is printed the residual (first iteration) or solution (later iterations) statistics.

If this solution is being done using the method of conjugate gradients, after the first (mathematically "zeroth") iteration only, the used normal matrix array (array "l1") size, in number of elements, is printed.

For the second and later iterations, the previous iteration solution standard deviation (SIG1, see below) is printed for comparison with this iteration's standard deviation.

For the second and later iterations, if the solution standard deviation has changed by less than  $10^{-6}$ , a message is also printed that says "Solution has CONVERGED."

Next, statistics are printed. For the first iteration these are actually just the statistics based on the residuals with no solution having been done. For later iterations they are the true solution statistics. These values are the standard deviations (in mm) for the line (or Y) measurements (SIGL), for the sample (or X) measurements (SIGM), for both (SIG1), and then as the a posteriori standard deviation of unit weight (SIG2), where:

$$\text{SIGL} = \sqrt{(\text{sum } Y^{*2}) / \text{NMEA}}$$

$$\text{SIGM} = \sqrt{(\text{sum } X^{*2}) / \text{NMEA}}$$

$$\text{SIG1} = \sqrt{((\text{sum } X^{*2} + \text{sum } Y^{*2}) / (\text{NMEA} * 2))}$$

$$\text{SIG2} = \sqrt{((\text{sum } X^{*2} + \text{sum } Y^{*2}) / (\text{NMEA} * 2 - \text{NUNK}))}$$

where X are the sample residuals, Y are the line residuals, and NMEA and NUNK are as in Group 1 above. Note that  $\text{NMEA} * 2 - \text{NUNK}$  can be zero or negative and yet a solution can be obtained if a sufficient number of

parameters are weighted. However, if this case occurs a warning is issued and SIG2 is set to 1.

Example (from che04.dat):

SIGL = 0.01045 SIGM = 0.01001 SIG1 = 0.01023 SIG2 = 0.01169

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Reference: Model, program, and format generally follow that specified in:

Colvin, Tim R. (1992). "Photogrammetric Algorithms and Software for Spacecraft Optical Imaging Systems," \_ A RAND NOTE \_, N-3330-JPL.

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Document History:

Begun 2006.08.10 by B. Archinal.

Modifications: Modified 2015.10.05 by G. Cushing for web release.

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(End of document.)